

Machine learning approach for link prediction in large stochastic online social networks (SOSNs)

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Abstract

Social networks are growing every day at a tremendous pace. A social network is an online community that allows users to interact and exchange ideas, information, activities, and interests. Millions of users are contributing to its character and behaviour, and the information being generated has a multitude of dimensional aspects that provide new opportunities and perspectives for the computation of network properties. Every individual quickly spreads messages and information throughout all linked groupings. Social networks give users the ability to make a profile, connect with others, and communicate with them through a variety of tools like chatting, updating their status, leaving comments, and sharing text, images, audio, and animated videos. With billions of users globally, social media platforms have emerged as an essential part of contemporary social interaction and communication. Along with changing how individuals share and consume information, they have also had a big impact on social, political, and cultural developments. These days, social communities, governmental agencies, and commercial enterprises all depend heavily on online social networks. Understanding networks' evolutionary nature requires the ability to predict missing links in existing networks and emerging or broken linkages in future networks. Since SNs undergo dynamic changes over time, link inference in these networks is an extremely difficult task. The dynamic character of supernovae is not well-accounted for in link prediction techniques. In this study, link prediction techniques in dynamic SNs will be thoroughly reviewed, analysed, discussed, and evaluated.

Keywords

Social Networks, Machine Learning, Social Communities

1. Introduction

Kleinberg and Liben-Nowell introduce the link prediction problem for Social Networks [SNs][1]. The challenge of link prediction is to determine, given the existing structure of a graph (sociogram or network), between which nodes and edge will develop following the disconnected nodes in future. So far, there has been some success in link prediction using traditional social network analysis criteria that are simple. This study uses a dataset gathered from messages exchanged on a dating social networking website to investigate the issue in greater detail. Social networks are crucial for grasping the nature of entities and human behavior. More than millions of peoples participating in more than one online-social networking application/sites, social network research has become significant attention [2]. A wealth of details can be found in SNs, which can be mined or examined to draw insightful conclusions.

The global connectivity enabled by online social networks has revolutionized the way we communicate, share information, and build relationships in the modern world. With the growing use and popularity of these platforms, researchers have begun employing various mathematical models to explore the dynamics and characteristics of these networks. One approach to understanding the friendships and communication patterns within these networks is the review of Stochastic Online Social Networks (SOSNs). Stochasticity, referring to randomness or uncertainty, suggests that individual behaviour and interactions are influenced by probabilistic factors [3,4]. Unlike traditional social network models, which assume consistent and predictable interactions, stochastic models account for the inherent unpredictability and variability in human behaviour within these virtual communities.

A SN is the outcome of a collection of individuals' diverse personal and social relationships. It can be used for a variety of purposes, such as political awareness campaigns, blogging, advertising, and review collection. Since SNs are always growing, they are extremely dynamic. Comprehending and optimizing the quantity of links is a primary concern in SNs, as it facilitates the effective utilization of SN services and ensures prompt information dissemination across the network. The method of determining the most likely linkages between disconnected nodes in a social network is known as link prediction[5,6,7]

With the rise of social media platforms like Facebook and Twitter, social network analysis has garnered significant interest. Social networks are dynamic structures composed of nodes (users) and edges (relationships). Link prediction, a key area in this field, aims to predict future connections based on current network characteristics [8]. Traditional methods are limited to static and homogeneous networks, necessitating advanced models for dynamic and heterogeneous networks.

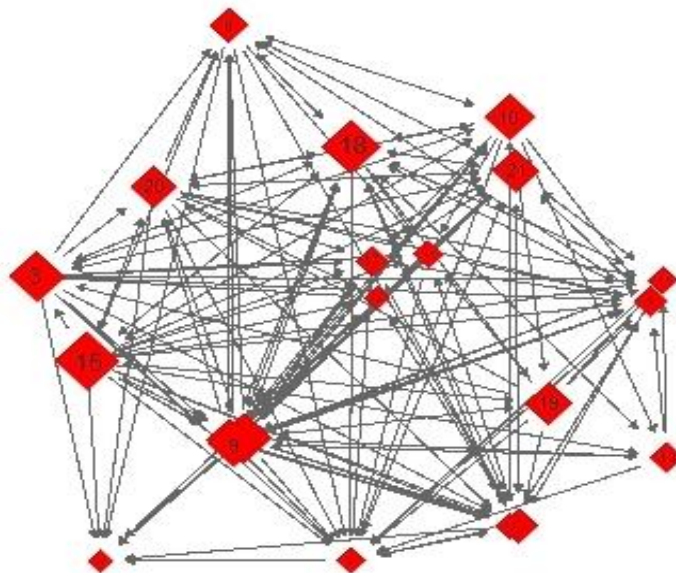


Figure 1. Social Network Representation by Directed Graph

2 Literature Review

The prediction of future links in social networks involves various methods using both local and global features. These methods typically compute a similarity measure between node pairs, which can be based on node features (like the number of adjacent nodes or common neighbors) or network topological features (like the path or distance between nodes) [9,10,11]. The performance of these methods varies because the features are independent, making it hard to define consistent similarity measures for predicting future links. To address performance gaps, probabilistic models learn from the social network, using local and global features as random variables approximated by Bayesian methods.

Alternative approaches include adjacency matrix recovery, which applies sparse matrix recovery or collaborative filtering. However, statistical models for link prediction in social networks are found to be more stable and accurate than matrix recovery approaches. Despite this, combining multiple approaches is suggested to improve link prediction [12,13].

Conventional node similarity methods and neural network techniques have been proposed for link prediction, especially for networks with multiple node types and dynamic links. For example, a multivariate NARX model was developed for predicting new and recurring links in heterogeneous networks, and a supervised link prediction model used meta-path features to support neural network models [14]. Another model used belief function theory to quantify link existence based on neighboring node information.

Network structural entities and their attributes can also derive similarity measures for potential node pairs [15,17]. A similarity measure using network motifs was developed within a supervised learning framework.

Despite extensive research, the dynamic and varied nature of online social networks (OSNs) means no single method can predict future connections accurately across all types of networks [16].

3 Machine Learning Techniques

3.1 Clusters

In order to find naturally occurring groupings within a dataset, clustering is a machine learning technique that divides data or objects into classes, groups, or clusters. This method can be used in a variety of fields, such as business research, social network analysis, and spatial data analysis. Euclidean distance is widely used by clustering algorithms to calculate the spatial separation between data objects and create clusters [18,19,20].

The complete network dataset, which consists of nodes and edges, is taken into consideration when social networks are utilised for link prediction [23]. Based on how similar certain features are among the nodes, clustering is done. These characteristics can be global (path distance between nodes) or local (node attributes). The method outlined focuses on analysing node attributes to identify similarity measures, which are subsequently utilised as clustering distance measurements [21,22].

3.2 Clustering methods

A clustering algorithm for link prediction in social networks typically involves several key steps, which include pre-processing the network data, computing similarity measures, clustering nodes based on these measures, and finally predicting potential links. Here's a general approach [65,66,67].

3.2.1. Data Pre-processing

Network Representation [23,24,25]: Represent the SNs as a graph $G=(V,E)$, where V is the set of nodes (users) and E is the set of edges (existing links between users).

Feature Extraction [26]: Extract relevant features from the nodes and edges. Features can be local (e.g., node degree, number of common neighbors) or global (e.g., shortest path distance between nodes).

3.2.2. Similarity Measurement

- Compute Similarity [27,28]: Calculate similarity scores between all pairs of nodes using chosen similarity measures. Common measures include:
 - Common Neighbors [29]: The number of shared neighbors between two nodes.
 - Jaccard Coefficient: The ratio of the intersection of neighbors to the union of neighbors.
 - Adamic/Adar Index [30]: A weighted measure that gives more importance to shared neighbors with fewer connections.
 - Preferential Attachment [31]: The product of the degrees of two nodes.

3.2.3. Clustering

Distance Metric: Use the similarity scores as a distance metric for clustering. Nodes with higher similarity scores are considered closer[32,33].

Clustering Algorithm: Apply a clustering algorithm to group similar nodes together. Common clustering algorithms include [34,35,36,37,38]:

- K-means Clustering: Partition nodes into k clusters based on similarity.
- Hierarchical Clustering: Create a dendrogram to represent nested clusters of nodes.
- DBSCAN (Density-Based Spatial Clustering of Applications with Noise): Cluster nodes based on density, identifying core samples and expanding clusters from them [39,40].

3.2.4. Link Prediction

- Potential Link Identification: Within each cluster, identify pairs of nodes that are not currently connected by an edge but have high similarity scores. These pairs are potential candidates for future links [41].
 - Prediction Model: Optionally, use a supervised learning model trained on existing links and non-links to improve prediction accuracy. Features for this model can include similarity measures and other node attributes [42,64].

4. Combined clustering approach

The proposed approach in this article combines two distinct link prediction methods to improve accuracy [43]. The methodology is twofold:

4.1 Phase One: Similarity Index Calculation

- Network nodes are processed, and neighborhood features are examined using Jaccard Coefficient (JC), Adamic/Adar Index (AA), and Preferential Attachment (PA) to generate a similarity index [44].
 - Scores for non-existing links are ranked to provide the probability of future link existence [45].

4.2 Phase Two: Clustering

An unsupervised k-means clustering technique is used to classify the network into clusters [46].

The k-means clustering technique is chosen for its speed and efficiency in processing large social networks [62,63].

4.3 Methodology Steps

- Input the social network dataset in the form of an edge list $G(u,v)$.
- Identify non-existing links between node pairs [48].
- Compute mutual neighbor nodes for every non-linked node pair.
- Compute the similarity features for each non-linked node pair.
- Sort the dataset in descending order based on similarity scores.
- Select an arbitrary centroid for the cluster node groups.
- Compute differences between centroids and similarity features, assigning nodes to the cluster where the difference is minimal.

5. Experimental results

This section deals with the assessment and comparison of the proposed solution to the link prediction problem [47,49,50]. Evaluation and comparison of PA,JC and AA shown below table 1.

Table 1. similarity measures for non-existing links and their corresponding clusters

Nodes(x,y)	JC	AA	PA	Custers
(1,4)	0.33	0.73	6	0
(1,5)	0.00	0.00	4	1
(2,4)	0.37	0.77	5	0
(2,5)	0.00	0.00	4	1
(3,5)	0.34	0.74	6	0

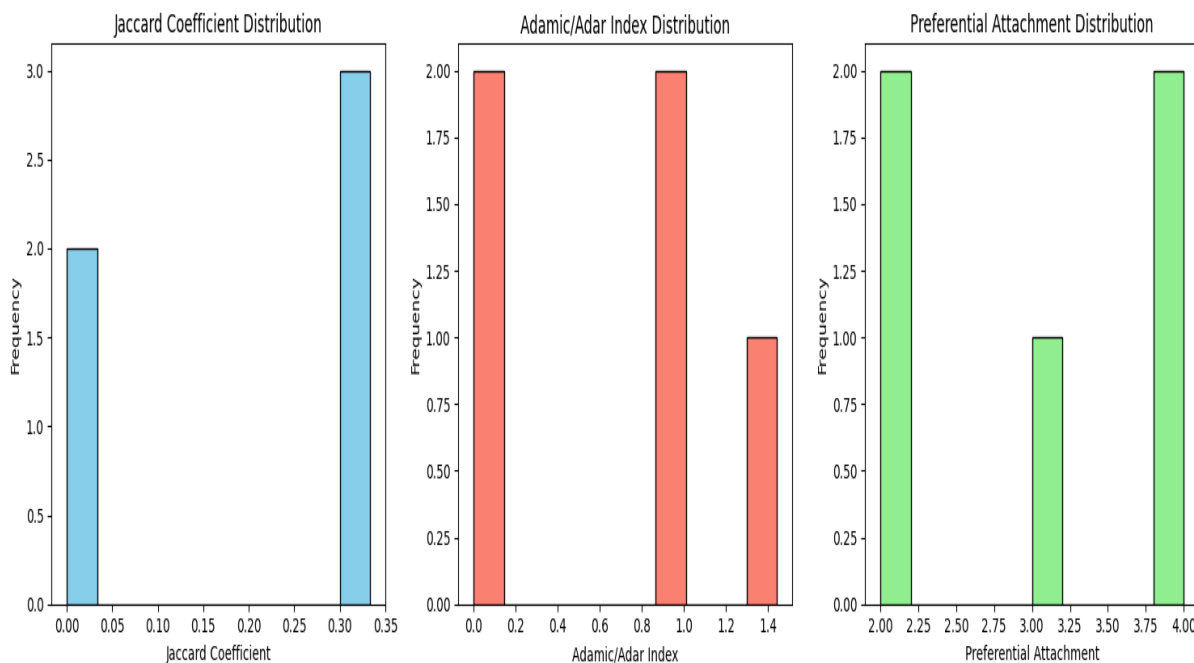


Figure 2. Representation of similarity measures using JC,AA and PA

4. Dataset used

In this paper we will use musae-wiki [68]. These datasets represent page-page networks on specific purpose. Nodes represent person and edges are mutual links between them. It contains 19,109 nodes and 400,832 links between nodes. This is an un-directed network.

7. Conclusion

This paper investigates link prediction in Online Social Networks (OSNs), highlighting the growing complexity due to the increasing size of these networks. It reviews various local feature-based similarity techniques and finds that they fall short as they focus only on local network features [51,52,53].

To address this, the article proposes a novel collaborative filtering-based approach to handle complex and large social network data. The method consists of two phases:

1. **Similarity Score Calculation[54,55]:** The first phase calculates similarity scores between non-linked node pairs using classical techniques-JC,AA and PA. This transforms the original network dataset into a feature-based network representation.
2. **Clustering and Link Prediction [56,57,58]:** The second phase uses k-means clustering on the transformed feature network to categorize nodes into clusters, predicting future links based on these clusters.

The proposed approach is more efficient than classical methods as it combines local feature-based techniques with clustering, reducing computational costs and memory usage. Future work will focus on evaluating the method's accuracy, expanding it to other social networks, and exploring additional unsupervised machine learning methods [59,60,61]. The approach also plans to incorporate considerations for outlier values that could influence results.

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